



Measures of Disease Frequency

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Introduction

- Measures of disease frequency are tools to describe how common an illness (or other outcome event) is with reference to the size of population at risk.
- Are used to quantify cases in relation to a population and a measure of time
- Outcome events of interest: infection, disease (morbidity), disability, death (mortality), recovery, presence of antibodies & usage of health services
- Two main measures: Prevalence & incidence

Introduction

- The measures can take various mathematical forms:
 - *Count* – Enumeration of the no. of cases of d'se or no. of persons affected with a condition in a given population. Often pop size is not accounted for hence counts are of limited use
 - *Proportion* – Ratio in which numerator is a subset of denominator e.g. if 200 persons are tested for TB and 40 are positive, the proportion positive is $40/200 = 0.2$ (20%). Prevalence & risk are both proportions.
 - *Odds* – Ratio in which numerator is not a subset of denominator e.g. 3 stillbirths and 120 live births, odds of stillbirth is $3:120 = 0.025:1$ or 25 stillbirths to 1000 live births. Odds of TB above is 40:160 or 1:4

Introduction

- The measures can take various mathematical forms:
 - *Rate* – Ratio in which denominator is the number of person-time units at risk e.g. 30 cases of pneumonia in an office of 100 people over a 3-month period, incidence rate is $30/(100*3) = 0.1$ cases per person-month. NB: $100*3 = 300$ person-months at risk. *Rate is generally used to refer to all types of measures of d'se frequency but should strictly be used to only refer to measures based on person-time units e.g. prevalence “rate”*

Incidence

- Concerned with quantifying the occurrence of *new cases*
- Two main measures of incidence – *risk & rate*

Incidence risk (cumulative incidence)

- Probability of occurrence of d'se in a d'se free population during a specified time period
- Given as:
$$\frac{\text{No. of new cases (d) in a defined period}}{\text{population at risk at start of study period (N)}}$$
- Since risk is a probability it ranges between 0 – 1 (0% –100%)
- Used for non-recurrent d'ses or applied to the 1st episode of a recurrent d'se

Incidence

Incidence risk (cumulative incidence)

- Restricted to closed populations (pop with no additions for duration of study and few to no losses [withdrawals])
- People lost to follow-up (withdrawals) are dealt with by subtracting half of no. of losses from pop at risk (assumed to be lost half-way through study period):

$$Risk = \frac{d}{N - (0.5 \times withdrawals)}$$

Examples:

- ❑ 15 out of 100,000 women developed cancer of the cervix in England in 1998
 - ❑ A study in Nairobi found 4 deaths of diarrhoea per 1,000 children per year
- Two other measures of risk:
 - ❑ *Attack rate* - defined as no. of new cases (d) occurring during duration of outbreak among a pop at risk at start of outbreak (N)
 - ❑ used in context of outbreaks/epidemics of infectious d'ses

Incidence

- *Secondary attack rate* - defined as proportion of those exposed to the primary case that develop d'se as a result of the exposure
 - Used in study of spread of infectious d'ses in small communities e.g. households or schools

Incidence rate (incidence density)

- Refers to no. of new cases of d'se in a population per person-time at risk
- It takes into account changes in size of pop at risk during the follow-up period
- Calculated as: $\text{Rate} = \frac{\text{No. of new cases of } d'se \text{ in a defined time period}}{\text{No. of person-time units at risk during the time period}}$

Incidence

Incidence rate (incidence density)

- Rate of new cases is hence related to a more precise measure of pop at risk during study period i.e. the *person-time units*
- The denominator thus accounts for the fact that some people who start at risk *do not remain* at risk during whole period because they develop the disease, or die or leave the pop by migrating, refusing to continue to participate in study etc.
- Others may join pop at risk after beginning of the period e.g. by birth, migration into area, recruitment into study etc.
- Can be calculated for d'ses with multiple episodes (recurrent)

Incidence

Incidence rate (incidence density)

- Appropriate for open populations – pop in which people are entering & leaving pop throughout study period
- Open pops can be stable if rates of additions and withdrawals are relatively constant over time

Example:

- Rate of diarrhoea in Ethiopia was 3.6 episodes per child-year
- The inverse of rate is an estimate of average time to occurrence of d'se if pop is closed or open & stable : $\frac{1}{Rate}$
- Exact & approximate methods available for calculating rate

Incidence

Incidence rate (incidence density)

- *Exact method* (exact amount of person-time at risk required) is preferred but info often unavailable

Example

- Assuming 4 previously healthy people were observed for exactly 1 month (30 days). The history for each individual was as follows:

1 person not sick at all	1.00 person-month at risk
1 person sick on day 10	0.33 person-months at risk
1 person sick on day 20	0.67 person-months at risk
1 person moved away on day 15 (and lost to follow-up)	0.50 person-months at risk
Total population at risk	2.50 person months at risk
Total new cases of disease	2
Incidence rate = $\frac{2}{2.5}$	0.80 cases per person-month

Incidence

Incidence rate (incidence density)

- In general: if risk period < study period use risk and if risk period > study period rate is appropriate
- Risk can be estimated from rate as follows:

$$\text{Risk} = 1 - \exp(-\sum \text{rates} * t)$$

Example

- Calculations based on deaths among 100 people in a nursing home experiencing a norovirus outbreak over 6 weeks are shown in the below table:

Week	Population at risk	Cases	Weekly incidence rate
1	100	1	0.0100 per person-week
2	99	2	0.0202 per person week
3	97	1	0.0103 per person week
4	96	3	0.0313 per person week
5	93	1	0.0108 per person week
6	92	0	0.0000 per person week
Total		8	0.0826

**The estimate of the
6-week risk is:**
 $1 - \exp(-\sum \text{rates} * t)$
 $= 1 - e^{(-0.0826)}$
 $= 0.079$ per 6 weeks

Prevalence

- Proportion of persons in a defined pop that have outcome of interest (existing cases) at a defined *instant (point)* in time (called **point prevalence**):

$$\text{Point prevalence} = \frac{\text{No. of existing cases at point in time}}{\text{Total pop at risk at same point in time}}$$

- We can also have **period prevalence** – calculated the same way as point prevalence except that:

$$\text{Period prevalence} = \frac{\text{No. of existing cases at any time during a specified time period}}{\text{Total pop at risk during the stated period}}$$

Prevalence

- Examples:
 - 1% of women having baby in a maternity hospital in Sao Paulo Brazil in 1999 were infected with HIV
 - The proportion of the population in India that has diabetes today

Relationship between Incidence & Prevalence

- If d'se is stable i.e. both incidence & duration of d'se are stable/constant over time, then prevalence is derived as:

$$\frac{p}{1-p} = \text{incidence} * \text{ave. duration of } d'se$$

- However, if prevalence is low (<10% of pop has d'se):

$$p = \text{incidence} * \text{ave. duration of } d'se$$

Relationship between Incidence & Prevalence

- Factors related to *duration* of d'se: subject's constitution, access to care, availability of treatment, social support & severity of d'se
- **NB:** Prevalence reflects factors not only related to d'se incidence but also those related to duration of d'se (survival with the disease) – so not appropriate for examining causal relationships

Uses of Incidence & Prevalence

- *Incidence:*
 - ❑ Estimate risk of d'se development
 - ❑ Study causal factors
 - ❑ Evaluate the effectiveness of primary prevention programs
- *Prevalence:*
 - ❑ Assist health care providers plan to deliver services
 - ❑ Indicate groups of people who should be targeted for control measures
 - ❑ May signal causal relationships, but also reflects determinants of survival

Other measures of d'se frequency

- Other than *attack rates* & *secondary attack rates* (described):
 - ❑ *Case fatality rate* – proportion of people with specific d'se that die from it (actually a risk)
 - ❑ *Infant mortality rate* – no. of deaths in children under one year of age divided by no. of live births in the same period in a specified pop (actually a ratio)
 - ❑ *Maternal mortality rate* – no. of maternal deaths divided by no. of women of reproductive age (15-49) in a specified year (also a ratio)
 - ❑ *Odds of d'se* – no. of cases in a defined pop and time period divided by no. of people who **did not become a case (non-cases)** in the time period
 - ❑ *Proportional morbidity/mortality* – used when appropriate denominator is unknown: no. of cases/deaths due to *specific d'se* divided by no. of cases/deaths from *all d'ses* diagnosed